II B. Tech I Semester Regular/Supplementary Examinations, October/November - 2018 PROBABILITY AND STATISTICS
(Civil Engineering)
Time: 3 hours
Max. Marks: 70
Note: 1. Question Paper consists of two parts (Part-A and Part-B)
2. Answer ALL the question in Part-A
3. Answer any FOUR Questions from Part-B

## PART -A

1. a) If the probability of a defective bolt is 0.2 find mean and standard deviation of the distribution of bolts in a total of 400
b) If probability density function is $f(x)=\left\{\begin{array}{cc}k x^{3} & \text { for } 0 \leq x \leq 3 \\ 0, & \text { elsewhere }\end{array}\right.$. Find the value of k and find the probability between $x=1 / 2$ and $x=3 / 2$
c) A random sample of size 100 has a standard deviation of 5 . What can you say about the maximum error with $95 \%$ confidence?
d) A random sample of size 25 from a normal population has the mean $\bar{X}=47.5$ and the standard deviation $\mathrm{S}=8.4$. Does this information tend to support or refute the claim that the mean of the population is $\mu=42.5$
e) Find mean values of X and Y from the following regression equations $2 \mathrm{Y}-\mathrm{X}-50=0,3 \mathrm{Y}-2 \mathrm{X}-10=0$
f) Measurements of average $\bar{X}$ and range $\bar{R}$ from 20 samples each of size 5 gave the following results $\bar{X}=99.6, \bar{X}=7.0$. Determine the vales of control limits for drawing a mean chart (Given that for $\mathrm{n}=5$, mean range 2.32Xpopulation standard deviation)

## PART -B

2. a) If a Poisson distribution is such that $3 P(X=1)=2 P(X=3)$. Find
b) The probability density function of a variate X is

| X | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{P}(\mathrm{X})$ | k | 3 k | 5 k | 7 k | 9 k | 11 k | 13 k |

Find (i) k (ii) $P(3<X \leq 6)$ (iii) what will be the minimum value of k so that $(X \leq 2)>0.3$ ?
3. a) The life of LED bulbs of a certain type may be assumed to be normally distributed with mean 155 hours and standard deviation 19 hours. Determine the probability that the life of a randomly chosen bulb
(i) is between 136 hours and 174 hours
(ii) less than 117 hours (iii) will be more than 395 hours
b) Define moment generating function and explain how moment generating function is used to obtain moments
4. a) Sample of size 2 are taken from the population $1,2,3,4,5,6$ with replacement. Find (a) the mean of the population (b) the standard deviation of the population (c) the mean of the sampling distribution of means and (d) the standard deviation of the sampling distribution of means
b) A random sample of size 81 was taken whose variance is 20.25 and mean is 32 , construct $98 \%$ confidence interval
5. a) In a certain factory there are two independent processes for manufacturing the same item. The average weight in a sample of 700 items produced from one process is found to be 250 gms with standard deviation of 30 gms while corresponding item in a sample of 300 items from the other process are 300 and 40 . Is there significant difference between the mean at $1 \%$ level.
b) 200 digits were chosen at random from a set of tables. The frequencies of digits are shown below

| Digit | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Frequency | 18 | 19 | 23 | 21 | 16 | 25 | 22 | 20 | 21 | 15 |

Use $\chi^{2}$ test to assess the correctness of the hypothesis that the digits were distributed in equal number in the tables from which these were chosen.
6. a) Fit a polynomial of second degree to the data points given below

| $x$ | 0 | 1 | 2 |
| :--- | :--- | :--- | :--- |
| $y$ | 1 | 6 | 17 |

b) Find the coefficient of correlation between X and Y

| X | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Y | 12 | 11 | 13 | 15 | 14 | 17 | 16 | 19 | 18 |

7. The following are the sample means and ranges for ten samples each of size 5 .

Construct $\bar{X}$ chart and $\bar{R}$ chart and determine whether the process is in control

| Sample | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Mean $\bar{X}$ | 20 | 34 | 45 | 39 | 26 | 29 | 13 | 34 | 37 | 23 |
| Range R | 23 | 39 | 15 | 05 | 20 | 17 | 21 | 11 | 40 | 10 |

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## PART -A

1. a) In eight throws of a die 5 or 6 is considered as success. Find the mean number of success and the standard deviation
b) The continuous random variable X has the probability density function
$f(x)=\left\{\begin{array}{cc}2 / x^{3}, & \text { if } 1<x<\infty \\ 0, & \text { otherwise }\end{array}\right.$. Find $\mathrm{F}(\mathrm{x})$
c) A research worker wants to determine the average time it takes a machine to rotate the tyres of a car and he wants to be able to assert with $95 \%$ confidence that the mean of the sample is off by at most 0.5 minutes. If we can presume from past experience that $\sigma=0.6$ minutes, how large a sample has to considered
d) A process of making certain ball bearings is under control if the diameters of the bearings have a mean of 0.5 cm . If the random sample of 10 of these bearings has a mean diameter of 0.5060 cm and standard deviation of 0.0040 cm , is the process under control?
e) Test whether the equations $2 x+3 y=4, x-y=5$ represent valid regression lines
f) A drilling machine bores holes with a mean diameter of 0.5230 cm and a standard deviation of 0.0032 cm . calculate the 2-sigma upper and lower control limits for means of samples 4.

## PART -B

2. a) If $2 \%$ of mobile phones of a company are defective, find the probability that (i) at least one defective (ii) exactly 7 defective (iii) at most 8 defectives in a sample of 100
b) From a lot of 10 items containing 3 defectives, a sample of 4 items is drawn at random. Let the random variable X denote the number of defective items in the sample. Find the probability distribution of X when the sample is drawn without replacement.
3. a) In a test of 1000 tube lights it was found that the life of a certain make was assumed to be normally distributed with an average life of 2040 hours and standard deviation of 60 hours. Find the number of tubes likely to burn for
(i) more than 2150 hours
(ii) less than 1950 hours and
(iii) more than 1920 hours and but less than 2160 hours
b) Find moment generating function of normal distribution
4. a) A population consists of five numbers $2,3,6,8,11$. Consider all possible samples of size two which can be drawn with replacement from this population. Find (a) the mean of population (b) the standard deviation of the population (c) the mean of the sampling distribution of means and (d) the standard deviation of the sampling distribution of means
b) A random sample of size 100 is taken from a population with standard deviation 5.1. Given that the sample mean is 21.6 . construct $95 \%$ confidence interval for the population
5. a) The mean height of 50 male students who participated in sports is 68.2 inches with standard deviation of 2.5 . The mean height of 50 male students who have not participated in sports is 67.2 inches with standard deviation of 2.8 . Test the hypothesis that the height of the students who participated in sports is more than the students who have not participated in sports.
b) Three samples each of size 5, were drawn from the three uncorrelated normal populations with equal variance. Test the hypothesis that population means are equal at $5 \%$ level.

| Sample 1 | Sample 2 | Sample 3 |
| :--- | :--- | :--- |
| 10 | 9 | 14 |
| 12 | 7 | 11 |
| 9 | 12 | 15 |
| 16 | 11 | 14 |
| 13 | 11 | 16 |

6. a) Obtain a relation of the form $y=\mathrm{a} b^{x}$ for the following data

| $x$ | 2 | 3 | 4 | 5 | 6 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $y$ | 8.3 | 15.4 | 33.1 | 65.2 | 127.4 |

b) Find Karl Pearson's coefficient of correlation from the following data

| Wages | 100 | 101 | 102 | 102 | 100 | 99 | 97 | 98 | 96 | 95 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Cost of <br> living | 98 | 99 | 99 | 97 | 95 | 92 | 95 | 94 | 90 | 91 |

7. The table below gives the sample means and ranges for ten samples each of size 5. Construct Control Charts for mean and range and test whether the process is in control or not

| Sample <br> No | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Mean | 4.9 <br> 8 | 4.9 <br> 2 | 5.0 <br> 2 | 4.9 <br> 8 | 4.9 <br> 8 | 5.0 <br> 8 | 5.0 <br> 4 | 4.9 <br> 5 | 4.9 <br> 5 | 4.9 <br> 2 |
| Range | 0.3 | 0.2 | 0.4 | 0.1 | 0.4 | 0.2 | 0.7 | 0.4 | 0.4 | 0.5 |

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## PART-A

1. a) If a random variable has a Poisson distribution such that $P(1)=P(2)$, find mean and variance of the distribution
b) Find the constant k such that
$f(x)=\left\{\begin{array}{ll}k x^{2}, & \text { if } 0<x<3 \\ 0, & \text { otherwise }\end{array}\right.$ is a probability function and find the distribution function $\mathrm{F}(\mathrm{x})$
c) If we can assert with $95 \%$ that the maximum error is 0.05 and $\mathrm{p}=0.2$ find the size of the sample
d) A die is tossed 960 times and it falls with 5 upwards 184 times. Is the die unbiased at the level of significance of 0.01 ?
e) If $\mathrm{X}=2 \mathrm{Y}+3$ and $\mathrm{Y}=\mathrm{kX}+6$ are the regression lines of X on Y and Y on X respectively. Then show that $0 \leq k \leq 1 / 2$
f) A drilling machine bores holes with a mean diameter of 0.5230 cm and a standard deviation of 0.0032 cm . calculate the 3 -sigma upper and lower control limits for means of samples 4 .

## PART -B

2. a) $20 \%$ of items produced from the factory are defective. Find the probability that in a sample of 5 chosen at random (i) none is defective (ii) one is defective (iii) $p(1<x<4)$
b) A random variable X has the following probability distribution

| X | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{P}(\mathrm{X})$ | k | 3 k | 5 k | 7 k | 9 k | 11 k | 13 k | 15 k | 17 k |

Determine (i) k (ii) $p(x<3)$ (iii) $p(x \geq 3)$ (iv) $p(0<x<5)$ (v) Find distribution function $F(x)$
3. a) The marks obtained in Concrete Technology by 1000 students are normally distributed with mean $78 \%$ and standard deviation $11 \%$. Determine
(i) how many students got marks above $90 \%$
(ii) what was the highest mark obtained by the lowest $10 \%$ of the students
(iii) within what limits did the middle of $90 \%$ of students lie
b) Find moment generating function of a random variable X having probability
4. a) A population consists of five numbers $4,8,12,20,24$. Consider all possible samples of size two which can be drawn with replacement from this population. Find (a) the mean of population (b) the standard deviation of the population (c) the mean of the sampling distribution of means and (d) the standard deviation of the sampling distribution of means
b) Measurements of the weights of a random sample of 200 ball bearings made by a certain machine during one week showed a mean of 0.824 and standard deviation of 0.042 . Find maximum error at $95 \%$ confidence interval. Find confidence limits of the mean if $x=32$.
5. a) In a big city 325 men out of 600 men were found to be smokers. Does this information support the conclusion that the majority of the men in this city are smokers?
b) Three different machines are used for a production. On the basis of the outputs, test whether the machines are equally effective.

| OUTPUTS | Machine 2 | Machine 3 |
| :--- | :--- | :--- |
| Machine 1 | 9 | 20 |
| 10 | 7 | 16 |
| 5 | 5 | 10 |
| 11 | 6 | 4 |
| 10 |  |  |

6. a) Determine the equation of a straight line which best fits for the data

| X | 10 | 12 | 13 | 16 | 17 | 20 | 25 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Y | 10 | 22 | 24 | 27 | 29 | 33 | 37 |

b) Calculate coefficient of correlation from the following data

| X | 12 | 9 | 8 | 10 | 11 | 13 | 7 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Y | 14 | 8 | 6 | 9 | 11 | 12 | 3 |

7. The following data are the sample means and ranges for ten samples each of size 5. Construct Control Charts for mean and range and comment on the nature of control

| Sample <br> No | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Mean | 12. <br> 8 | 13. | 13. | 12. | 13. | 14. | 12. | 15. | 13. | 14. |
| Range | 2.1 | 3.1 | 3.9 | 2.1 | 1.9 | 3.0 | 2.5 | 2.8 | 2.0 | 2.5 |

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## PART -A

1. a) A car-hire firm has two cars which it hires day by day. The number of demands for a car on each day is distributed as a Poisson distribution with mean 1.5. Calculate proportion of days on which there is no demand in an year.
b) If X is a continuous random variable with probability density function $f(x)=\left\{\begin{array}{ll}x^{2}, & \text { if } 1 \leq x \leq 1 \\ 0, & \text { otherwise }\end{array}\right.$. If $P(c \leq x \leq 1)=19 / 81$. Find the value of $c$.
c) It is desired to estimate the mean time of continuous use until an answering machine will first require service. If it can be assumed that $\sigma=60$ days, how large a sample is needed so that one will be able to assert with $90 \%$ confidence that the sample mean is off by at most 10 days.
d) A sample of 64 students have a mean weight of 70 kgs . Can this be regarded as a sample from a population with mean weight 56 kg . and standard deviation 25 kg .
e) If $\mathrm{X}=2 \mathrm{Y}+3$ and $\mathrm{Y}=\mathrm{kX}+6$ are the regression lines of X on Y and Y on X respectively. If $k=1 / 8$ find $r$
f) Explain the term statistical control. Discuss its aspects and advantages.

## PART -B

2. a) Probability that Ms.Uma hits a target is $1 / 2$. She fires 6 times. Find the probability that she hits the target (i) exactly 2 times (ii) more than 4 times (iii) at least once.
b) A random variable X has the following probability function

| X | -3 | -2 | -1 | 0 | 1 | 2 | 3 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{P}(\mathrm{X})$ | k | 0.1 | k | 0.2 | 2 k | 0.4 | 2 k |

Find (i) k (ii) Mean (iii) Variance
3. a) 1000 students have written an examination the mean of the test is 35 and standard deviation is 5 . Assuming the distribution to be normal, find
(i) how many students marks lie between 25 and 40
(ii) how many students get more than 40
(iii) how many students get below 20
(iv) how many students get more than 50
b) Find moment generating function of a random variable X having probability density function $f(x)=\left\{\begin{array}{rr}\frac{1}{3}, & \text { if }-1<x<1 \\ 0, & \text { elsewhere }\end{array}\right.$ 1 of 2
4. a) Sample of size 2 are taken from the population $3,6,9,15,27$ with replacement.

Find (a) the mean of the population (b) the standard deviation of the population (c) the mean of the sampling distribution of means and (d) the standard deviation of the sampling distribution of means
b) In a sample of 100 packages shipped by air freight 13 had some damage. Construct $95 \%$ confidence interval for the true proportion of damage package
5. a) In a hospital 480 females and 520 male babies were born in a week. Does these figures confirm the hypothesis that males and females are born in equal number?
b) A die is thrown 264 times with the following results. Show that the die is biased. [ Given $\chi^{2}{ }_{0.05}=11.07$ for 5 degrees of freedom]

| No. Appeared on the die | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Frequency | 40 | 32 | 28 | 58 | 54 | 52 |

6. a) Fit a curve $y=a e^{b x}$ to the data points given below

| x | 0 | 2 | 4 |
| :--- | :--- | :--- | :--- |
| y | 5.1 | 10 | 31.1 |

b) Calculate coefficient of correlation for the data

| X | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Y | 15 | 16 | 14 | 13 | 11 | 12 | 10 | 8 | 9 |

7. The following data gives readings 10 samples of size 6 each in the production of a certain component.

| Sample | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Mean $\bar{X}$ | 383 | 508 | 505 | 582 | 557 | 337 | 514 | 61 <br> 4 | 707 | 753 |
| Range R | 95 | 128 | 100 | 91 | 68 | 65 | 148 | 28 | 37 | 80 |

Draw Control Charts for $\bar{X}$ ( for $n=6, A_{2}=0.483$ ). What is your conclusion

